

CRS stacking: a simplified explanation

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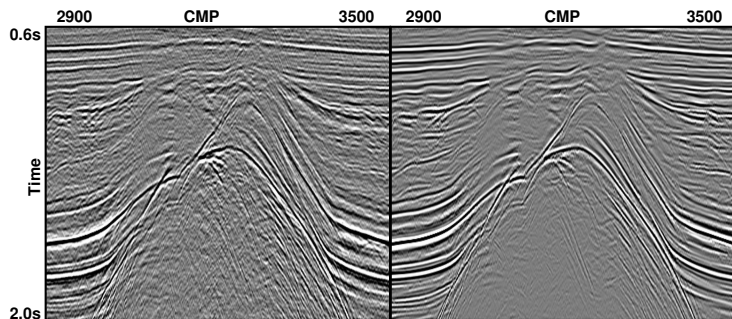
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Data example



conventional stack
(no postprocessing)

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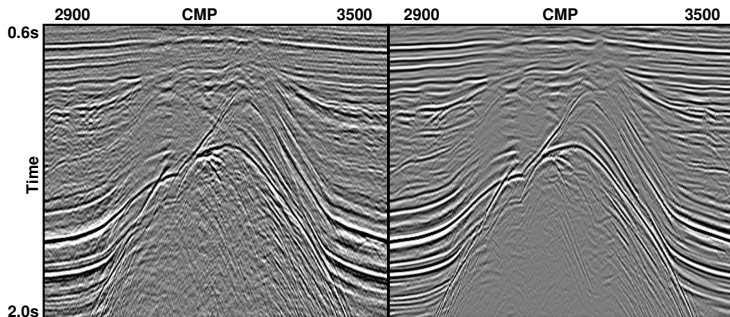
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- ▶ increased signal-to-noise ratio

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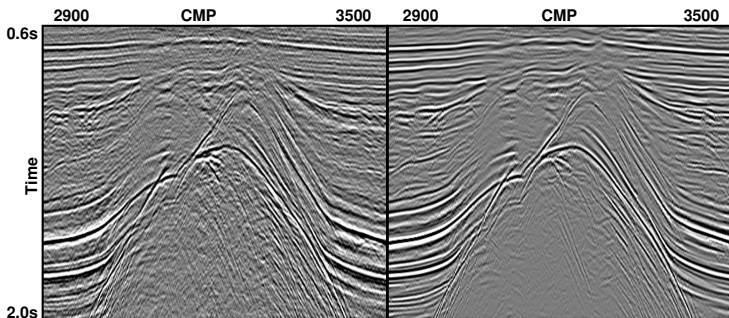
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CRS stack

- ▶ increased signal-to-noise ratio
- ▶ improved reflection event continuity

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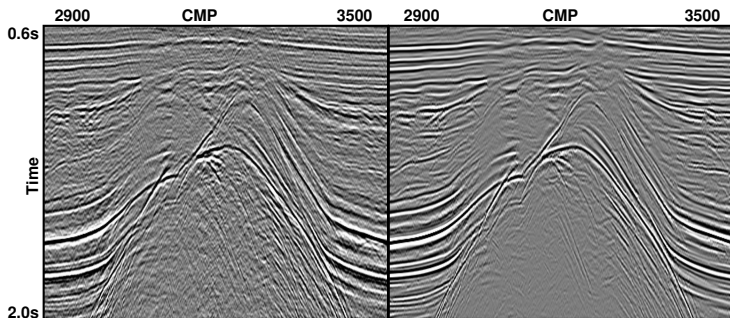
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- ▶ increased signal-to-noise ratio
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- ▶ additional stacking parameters

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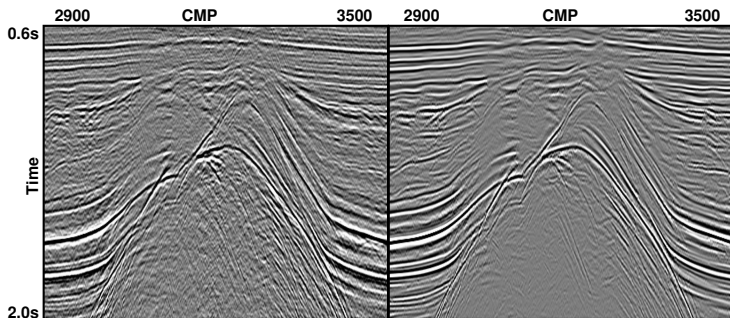
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Data example

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conventional stack
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CRS stack

- ▶ increased signal-to-noise ratio
- ▶ improved reflection event continuity
- ▶ additional stacking parameters
 - ↳ inversion, projected Fresnel zone, geometrical spreading, ...

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Conventional approach

Stacking velocity analysis and CMP stack

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Conventional approach

Stacking velocity analysis and CMP stack

- ▶ performed in CMP gathers only

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Conventional approach

Stacking velocity analysis and CMP stack

- ▶ performed in CMP gathers only
- ▶ based on analytic traveltime approximation, e. g.

$$t^2(x) = t_0^2 + \frac{x^2}{V_{\text{NMO}}^2},$$

x : offset, t_0 zero-offset travelttime

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- ▶ stacking velocity v_{NMO} usually picked manually assisted by coherence analysis

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Further implicit assumptions?

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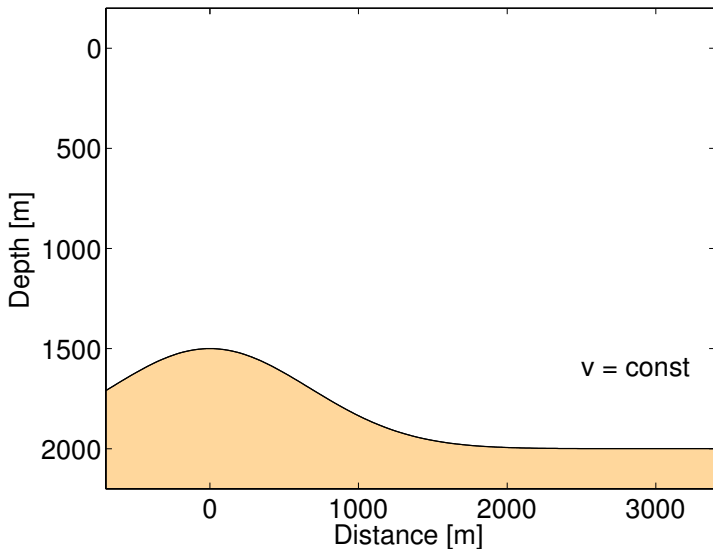
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Overlap of CMP illuminations



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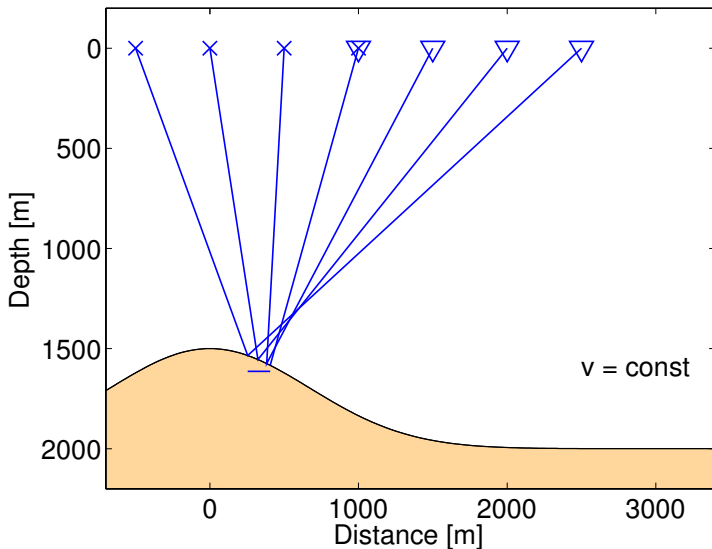
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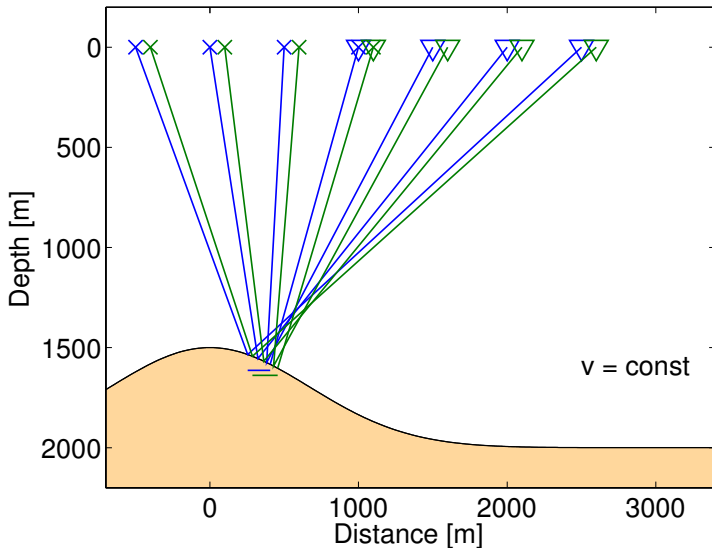
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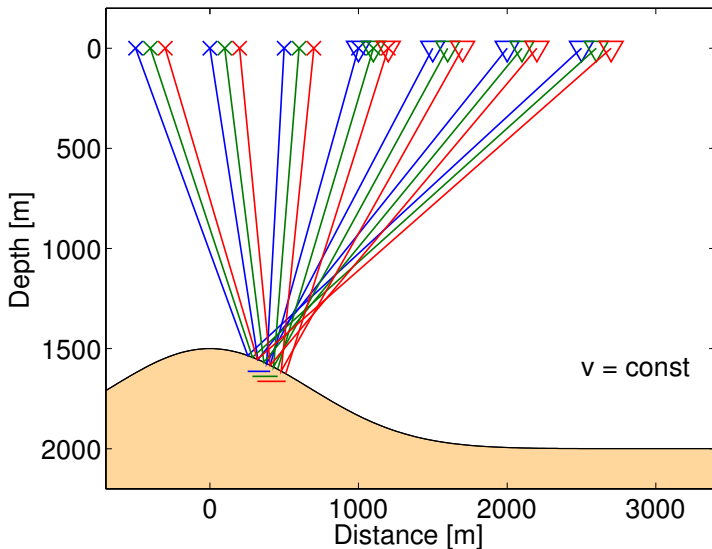
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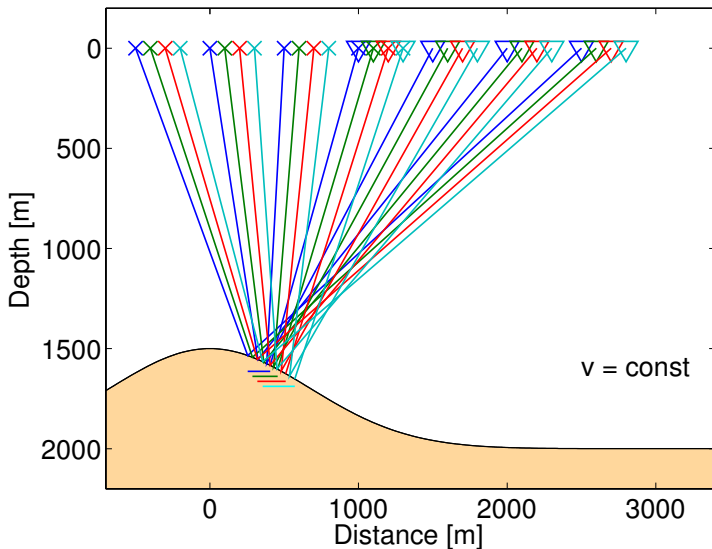
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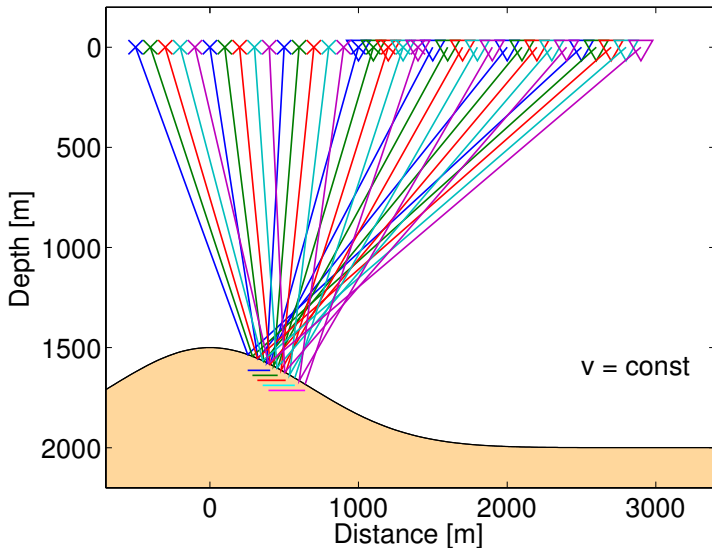
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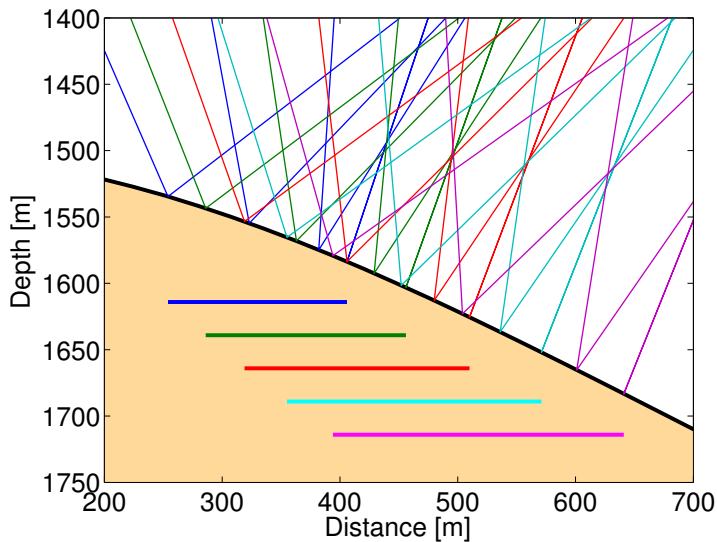
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Basic idea

Observations:

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Basic idea

Observations:

- ▶ conventional stack implicitly relies on reflector continuity

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Observations:

- ▶ conventional stack implicitly relies on reflector continuity
(this also applies to NMO + DMO correction)

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Observations:

- ▶ conventional stack implicitly relies on reflector continuity
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↳ Fresnel zone concept

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Consequences:

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If conventional stack works

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If conventional stack works

- ▶ there are neighboring reflection points

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- ▶ they physically contribute to the wavefield at a considered CMP

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If conventional stack works

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Why shouldn't we incorporate these
neighboring reflection points?

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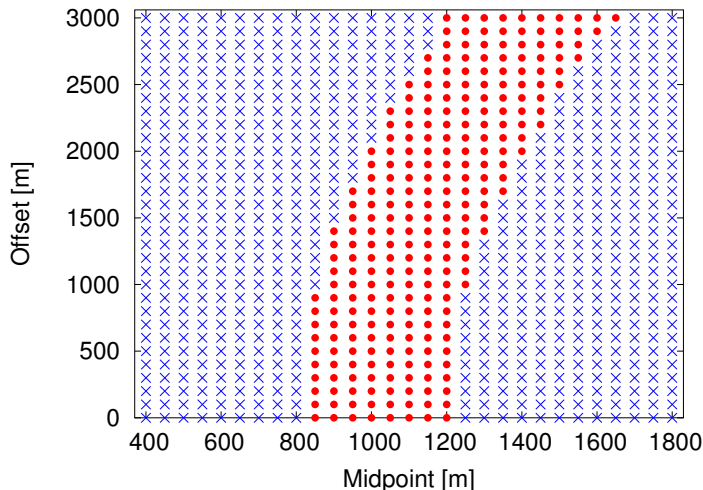
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Coverage of one CMP ray family



Traces with reflection points on reflector area illuminated by one CMP ray family

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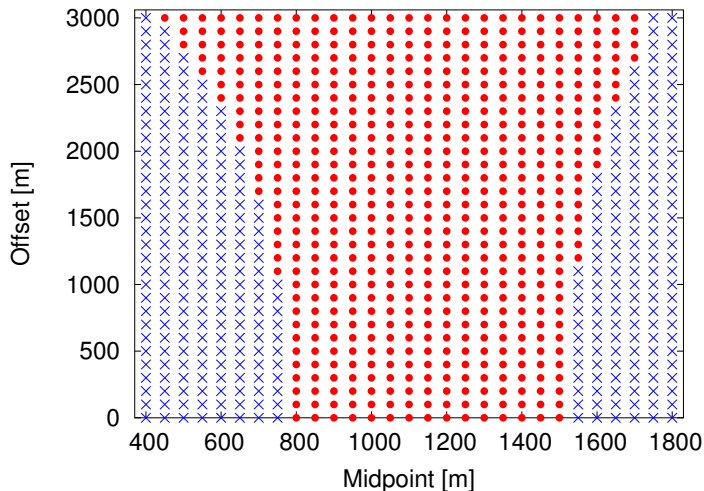
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Projected Fresnel zone



Projected Fresnel zone of the reflector area illuminated by one CMP ray family

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Features inherited from conventional stack:

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CRS stack

Features inherited from conventional stack:

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Features inherited from conventional stack:

- ▶ normal ray concept
- ▶ assumption of reflector continuity

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CRS stack

Features inherited from conventional stack:

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- ▶ analytical traveltimes approximation (2nd order)

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Additional features:

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Additional features:

- ▶ incorporates neighboring CMP gathers

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- ▶ yields additional stacking parameters
- ▶ increases the coverage

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Additional features:

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- ▶ yields additional stacking parameters
- ▶ increases the coverage
- ▶ improves reflector continuity and S/N ratio

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CRS stacking parameters

CRS stacking operator usually parameterized
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+ vivid geometrical interpretation

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- + vivid geometrical interpretation
- + useful for inversion, smoothing, . . .

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Aims in the following:



CRS stacking parameters

CRS stacking operator usually parameterized in terms of wavefield attributes

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Aims in the following:

- ▶ operator expressed in more familiar terms



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Aims in the following:

- ▶ operator expressed in more familiar terms
- ▶ demonstrate relation between these parameters



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Aims in the following:

- ▶ operator expressed in more familiar terms
- ▶ demonstrate relation between these parameters
- ▶ clear distinction between model and data space



CRS stacking operator

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CRS stacking operator

Hyperbolic representation:

$$t^2(\Delta m, x) = [t_0 + 2p\Delta m]^2 + \frac{x^2}{v_{\text{NMO}}^2} + \frac{\Delta m^2}{v_{\text{CMO}}^2}$$

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Δm midpoint displacement $m - m_0$

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Δm midpoint displacement $m - m_0$
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p horizontal slowness

v_{CMO} curvature-moveout velocity

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Hyperbolic representation:

$$\begin{aligned}t^2(\Delta m, x) &= [t_0 + 2p\Delta m]^2 + \frac{x^2}{v_{\text{NMO}}^2} + \frac{\Delta m^2}{v_{\text{CMO}}^2} \\&= \underbrace{t_0^2 + \frac{x^2}{v_{\text{NMO}}^2}}_{\text{conventional stack}} + \underbrace{4t_0 p\Delta m + 4\Delta m^2 p^2}_{\text{dip dependent}} \\&\quad + \underbrace{\frac{\Delta m^2}{v_{\text{CMO}}^2}}_{\text{curvature dependent}}\end{aligned}$$

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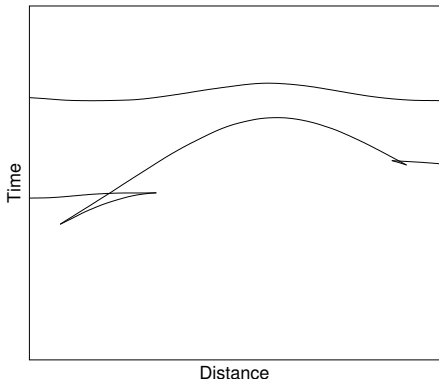
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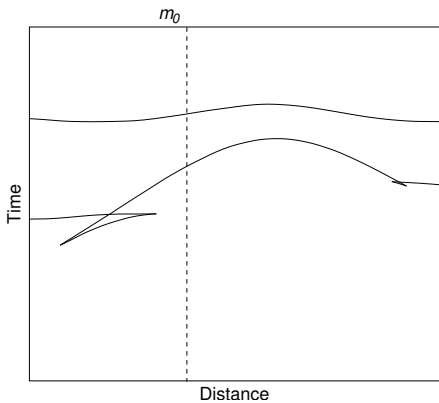
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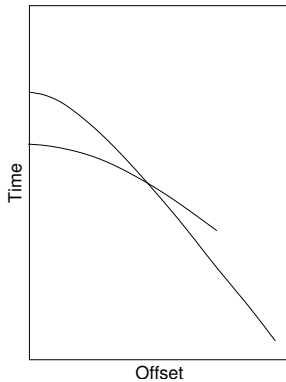
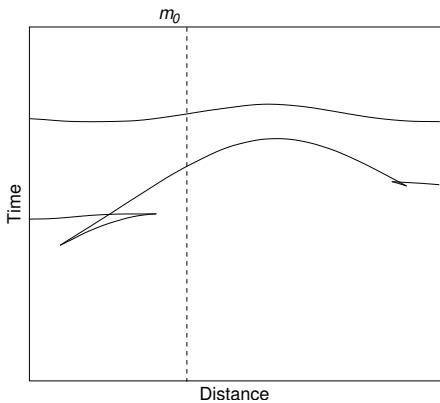
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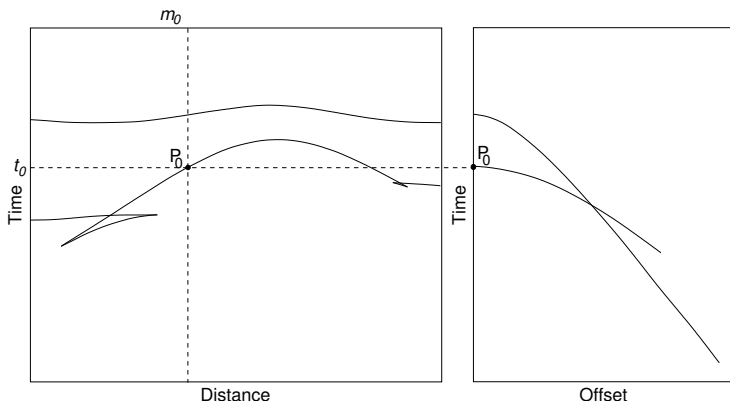
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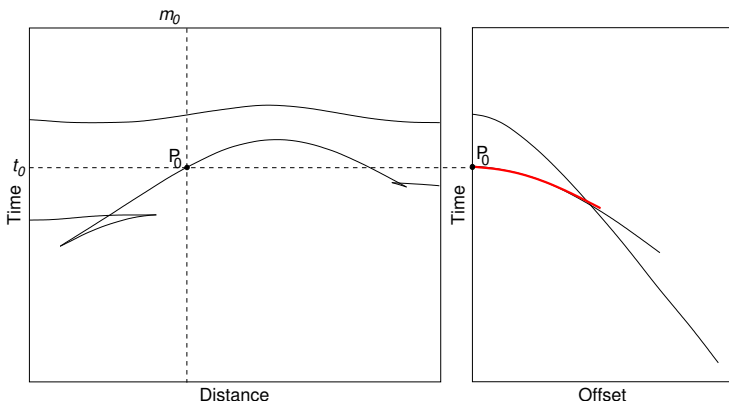
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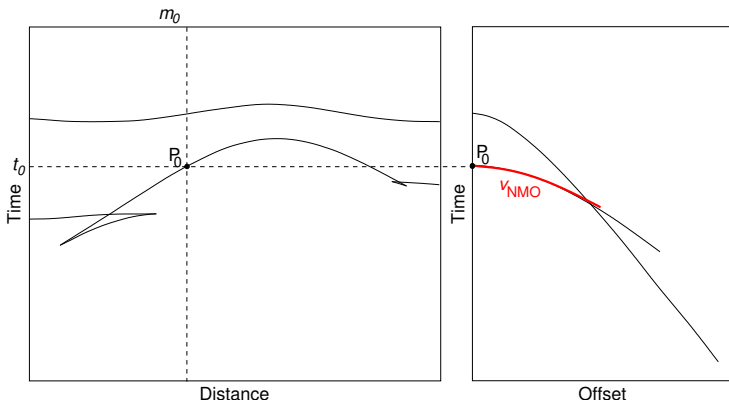
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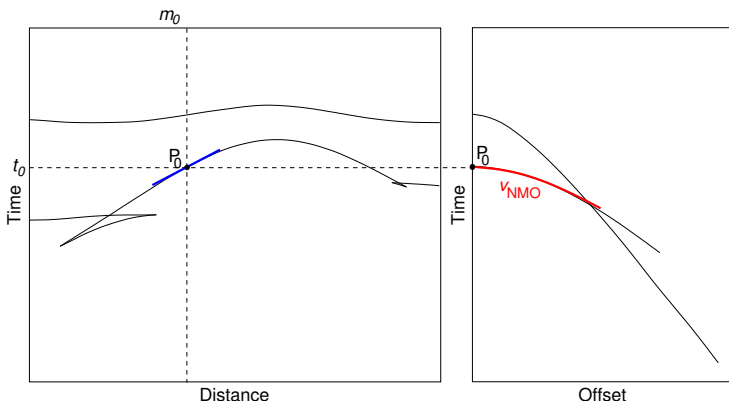
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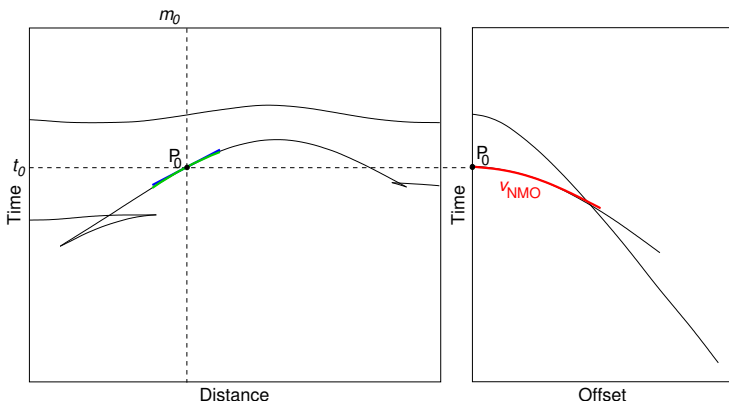
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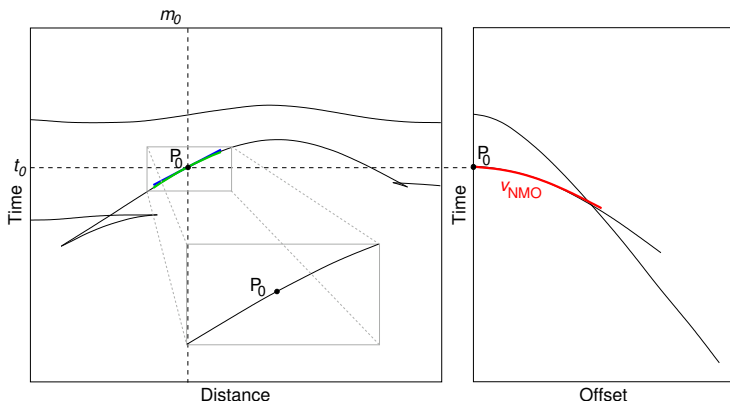
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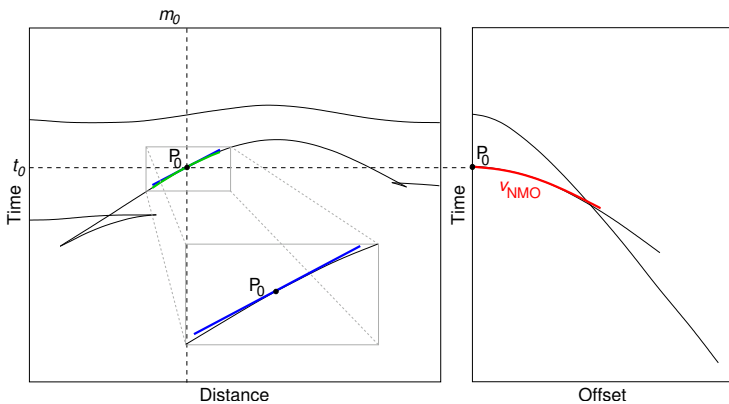
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CRS stacking: a simplified explanation

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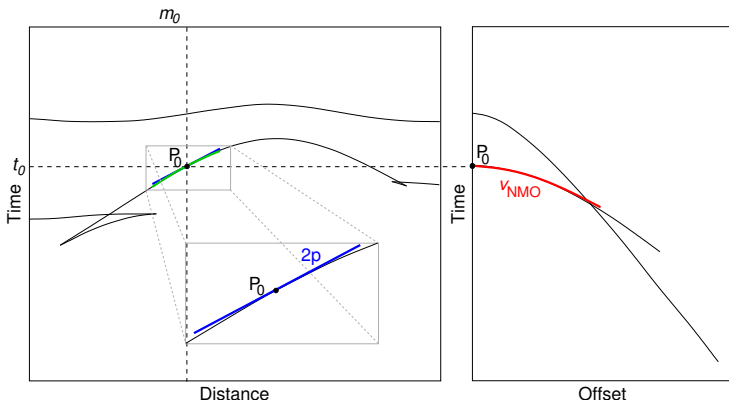
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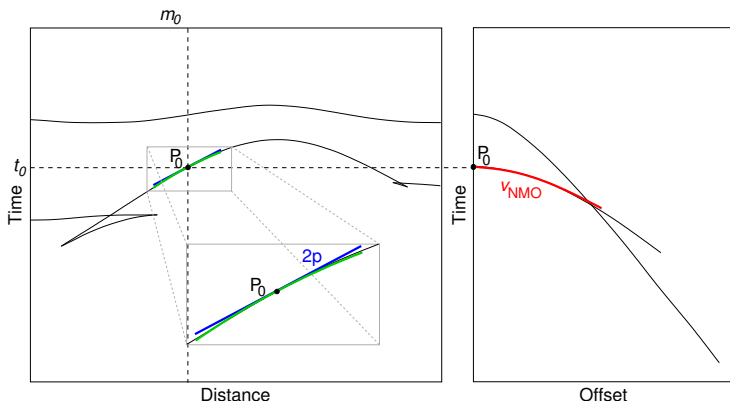
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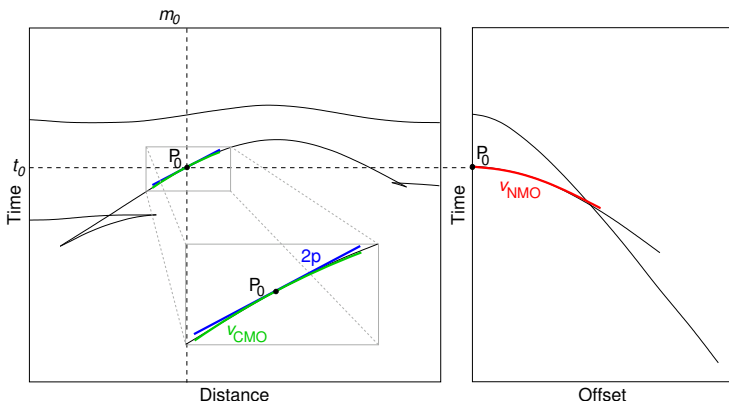
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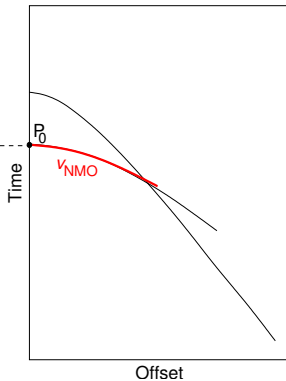
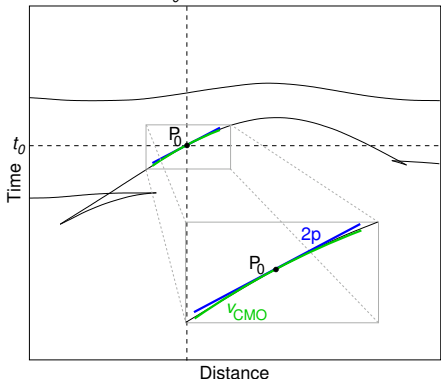
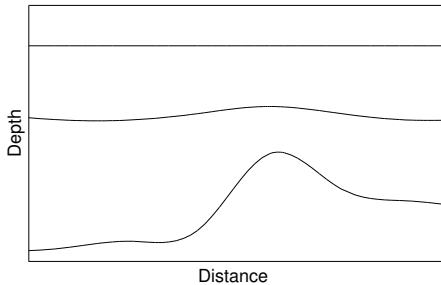
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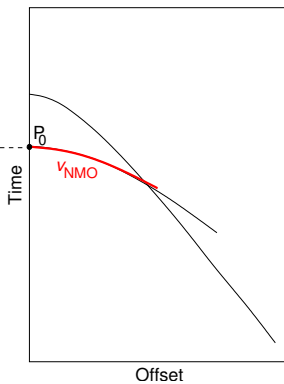
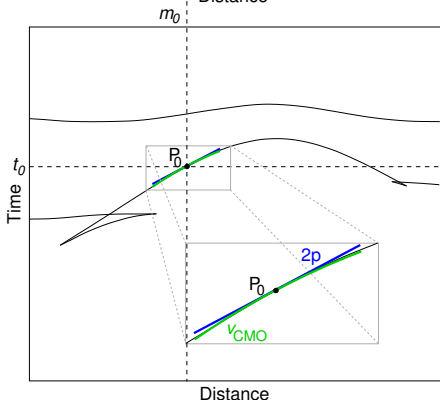
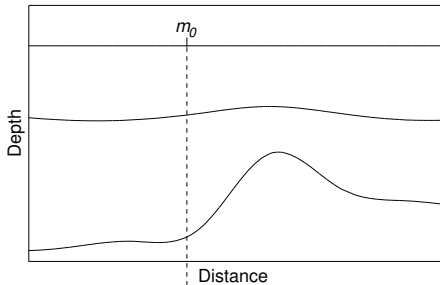
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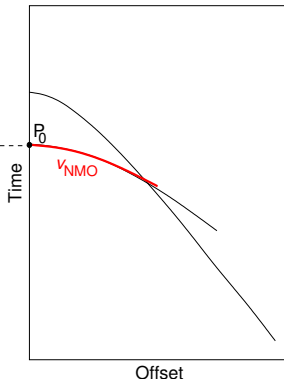
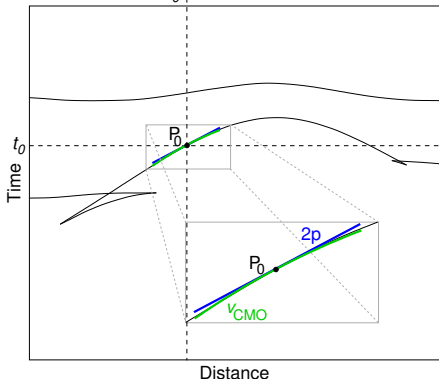
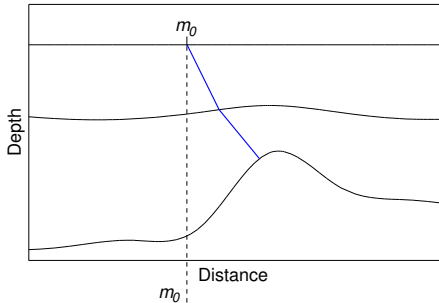
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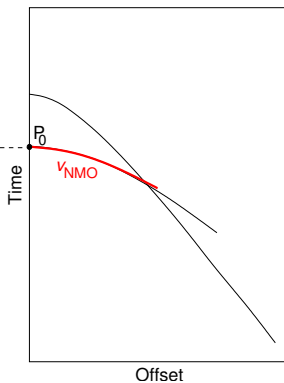
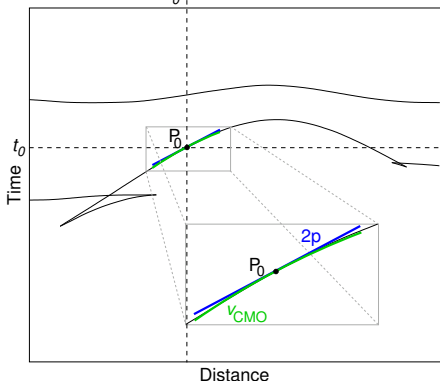
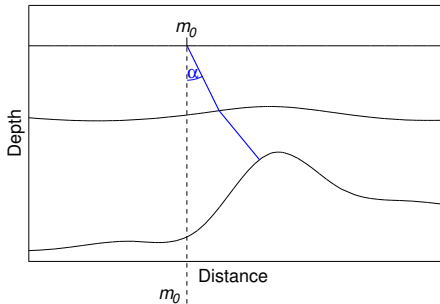
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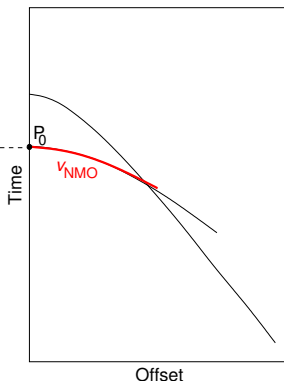
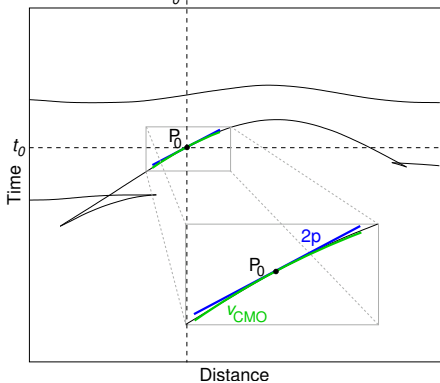
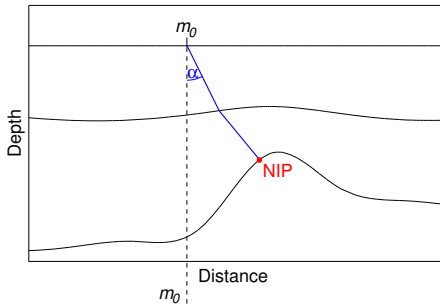
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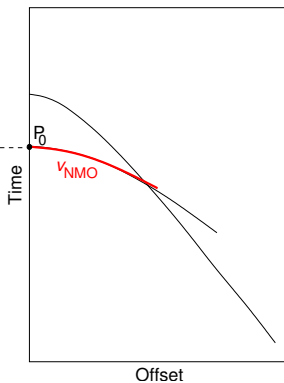
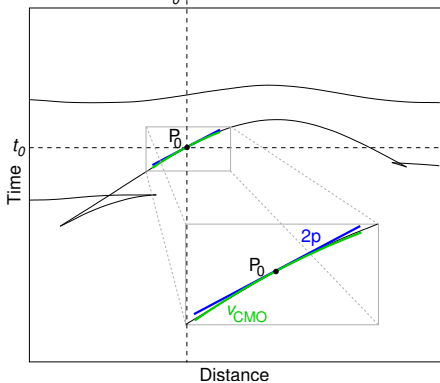
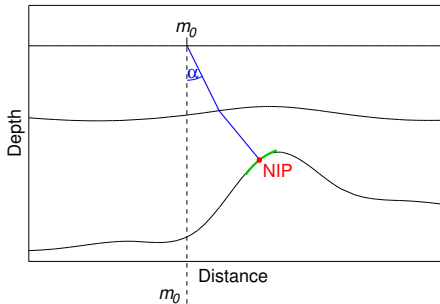
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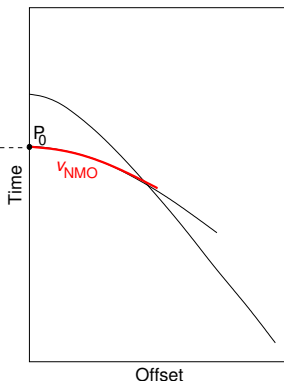
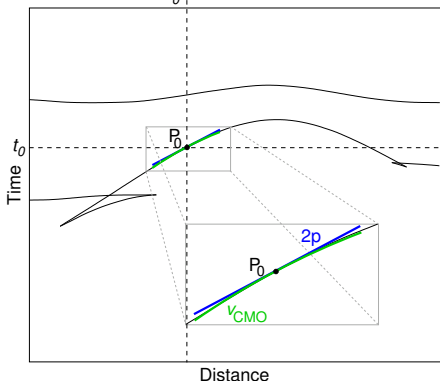
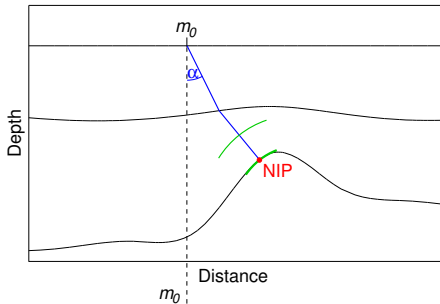
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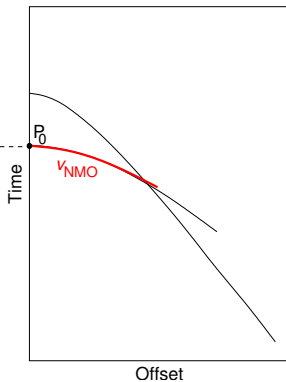
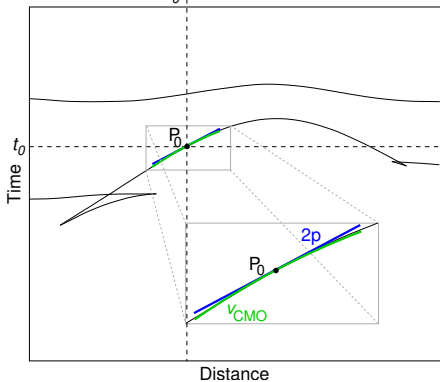
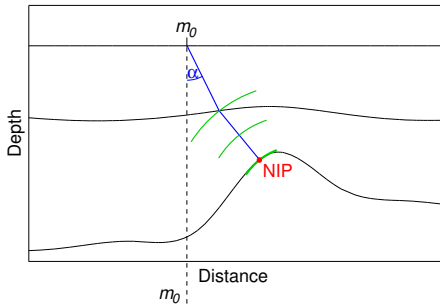
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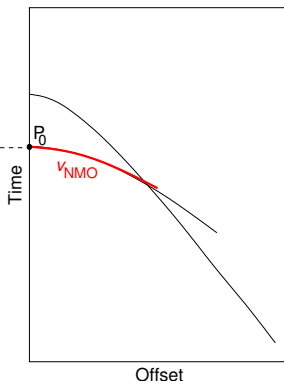
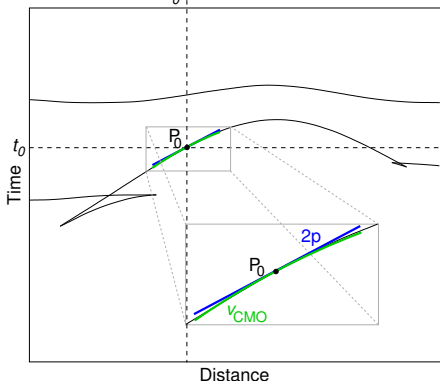
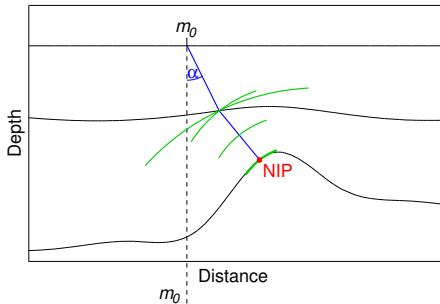
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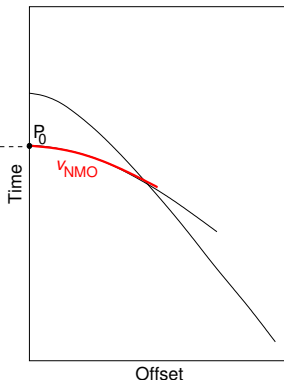
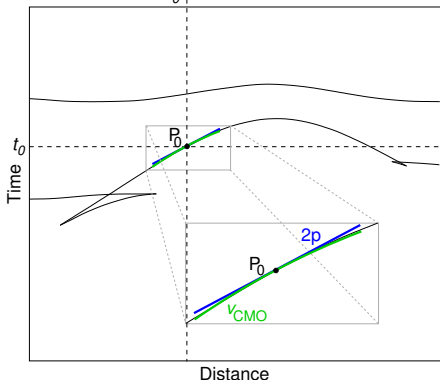
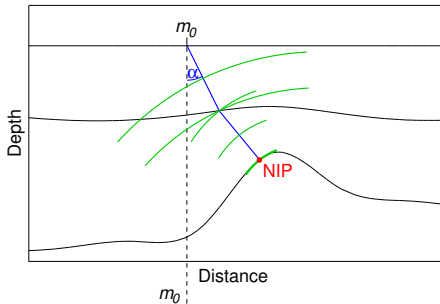
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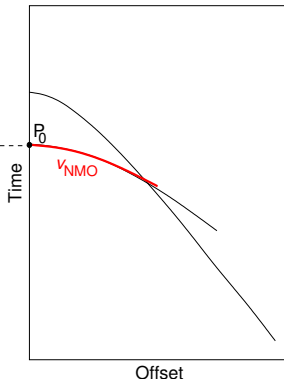
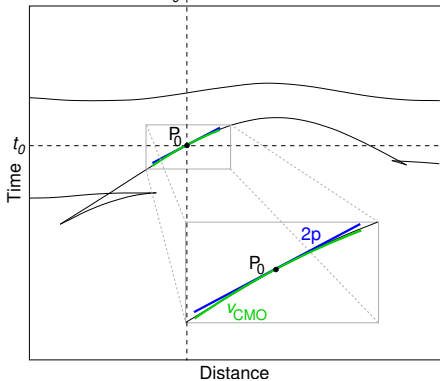
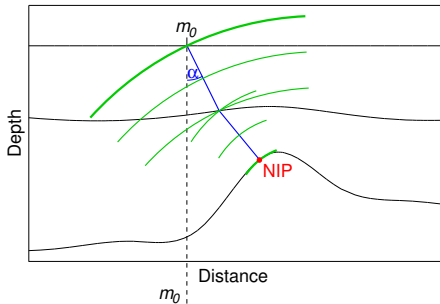
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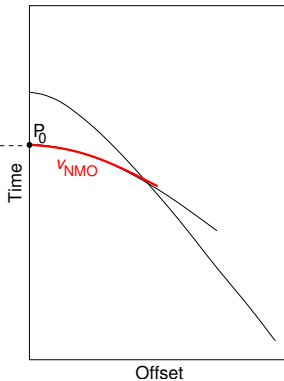
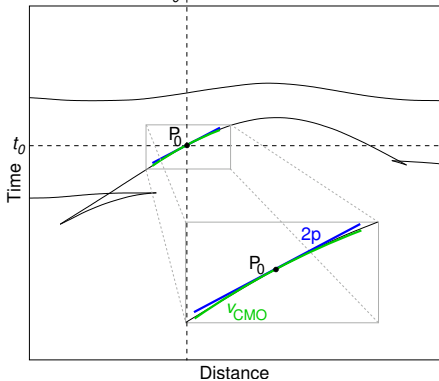
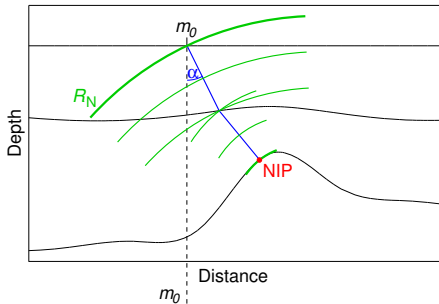
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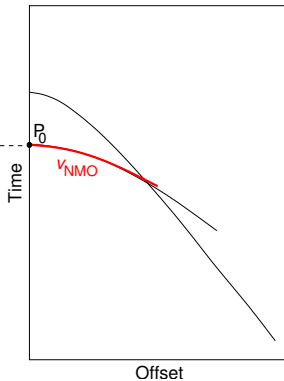
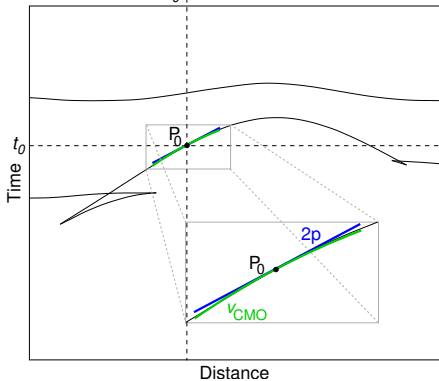
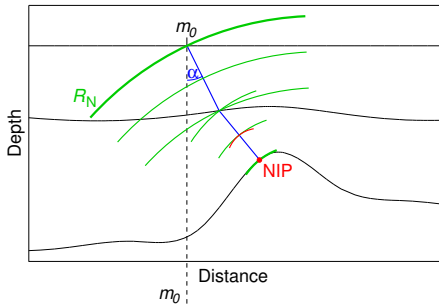
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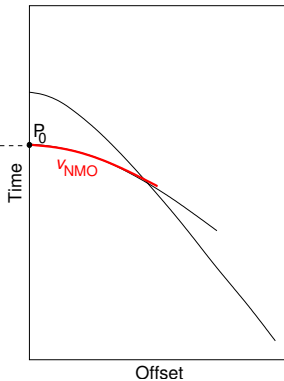
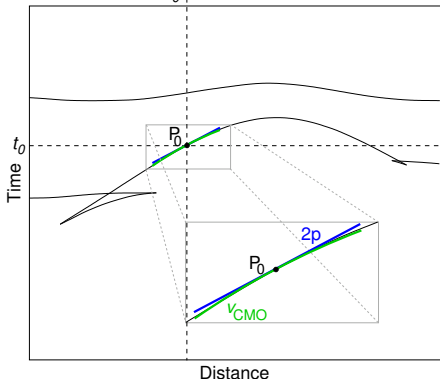
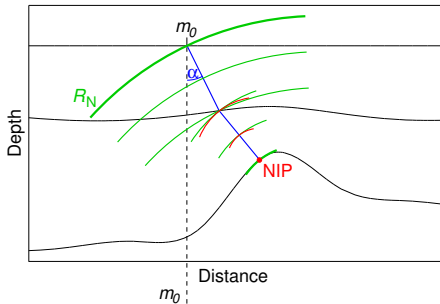
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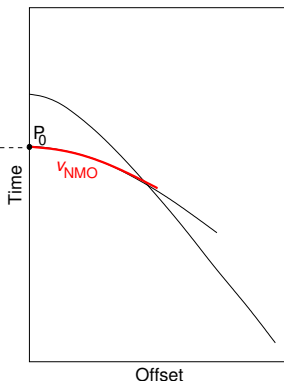
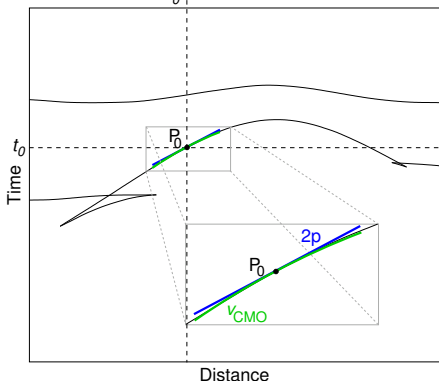
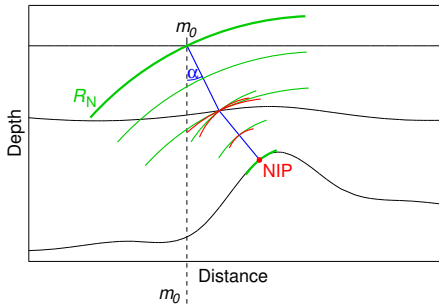
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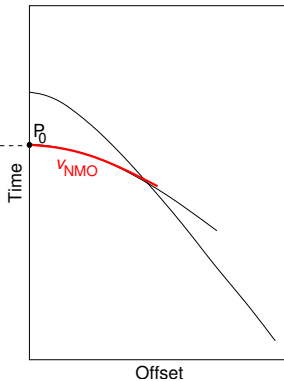
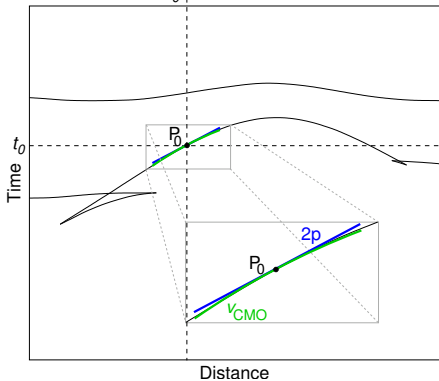
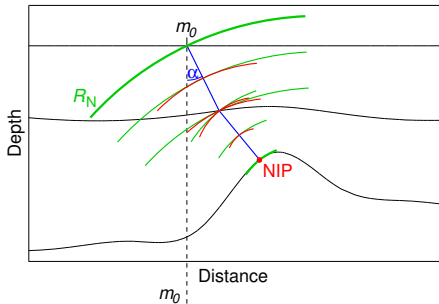
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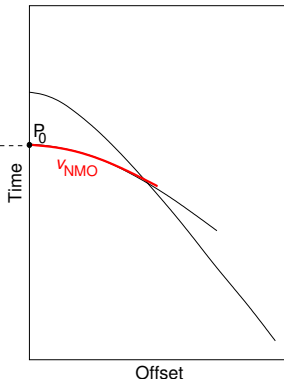
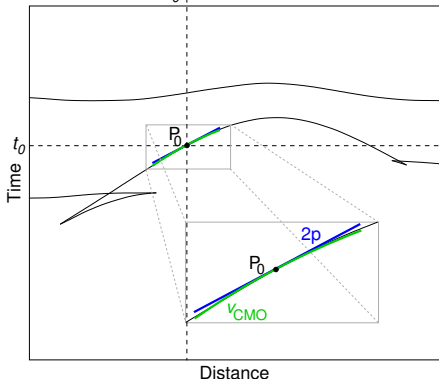
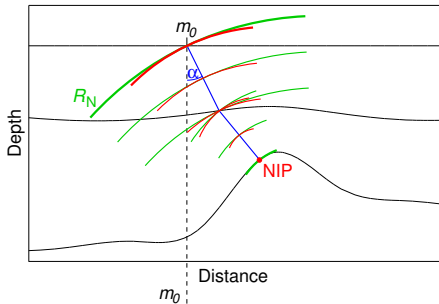
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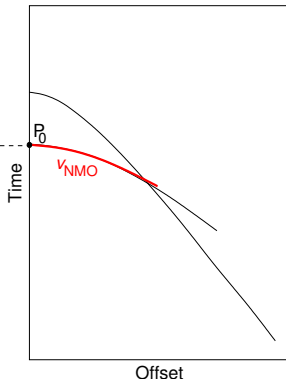
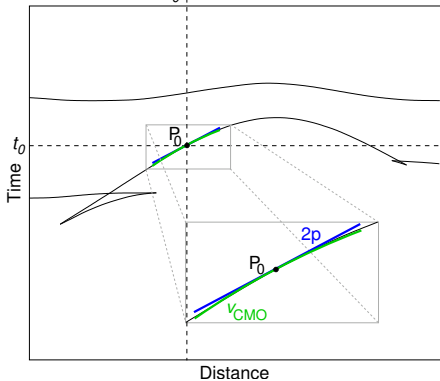
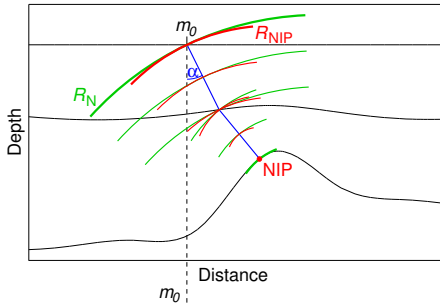
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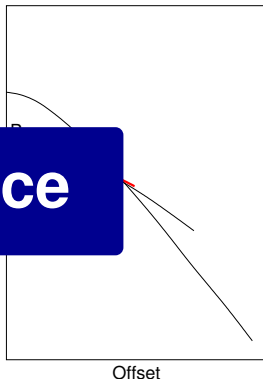
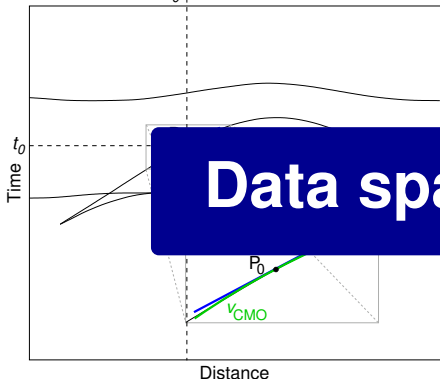
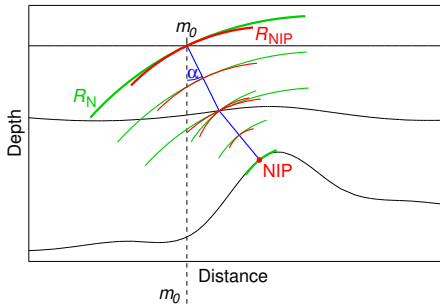
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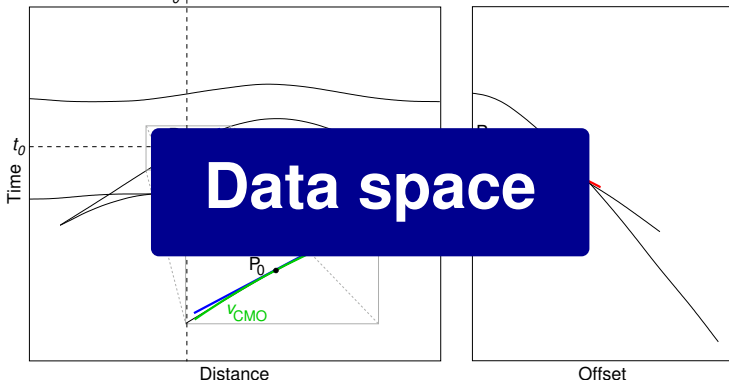
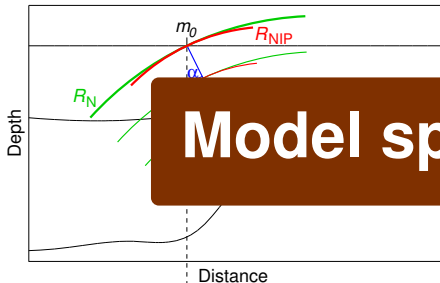
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Data space





Relations between parameters

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Parameterization in terms of...		
traveltime derivatives	wavefront properties	slowness and velocities



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Parameterization in terms of ...

traveltime
derivatives

wavefront
properties

slowness and
velocities

$$\left. \frac{\partial t}{\partial m} \right|_{m=m_0, x=0}$$

$$\frac{\sin \alpha}{v_0}$$

p

v_0 : near surface velocity



Relations between parameters

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Parameterization in terms of...

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$$\left. \frac{\partial t}{\partial m} \right|_{m=m_0, x=0}$$

$$\frac{\sin \alpha}{v_0}$$

p

$$\left. \frac{\partial t}{\partial m}, \frac{\partial^2 t}{\partial m^2} \right|_{m=m_0, x=0}$$

$$\frac{\cos^2 \alpha}{v_0 R_N}$$

v_{CMO}

v_0 : near surface velocity



Relations between parameters

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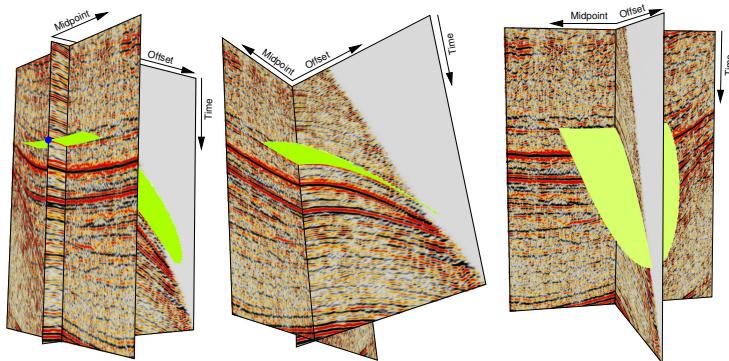
Parameterization in terms of...

traveltime derivatives	wavefront properties	slowness and velocities
$\left. \frac{\partial t}{\partial m} \right _{m=m_0, x=0}$	$\frac{\sin \alpha}{v_0}$	p
$\left. \frac{\partial t}{\partial m}, \frac{\partial^2 t}{\partial m^2} \right _{m=m_0, x=0}$	$\frac{\cos^2 \alpha}{v_0 R_N}$	v_{CMO}
$\left. \frac{\partial t}{\partial m}, \frac{\partial^2 t}{\partial x^2} \right _{m=m_0, x=0}$	$\frac{\cos^2 \alpha}{v_0 R_{\text{NIP}}}$	v_{NMO}

v_0 : near surface velocity



CRS operator



CMP gather and section at offset 500 m

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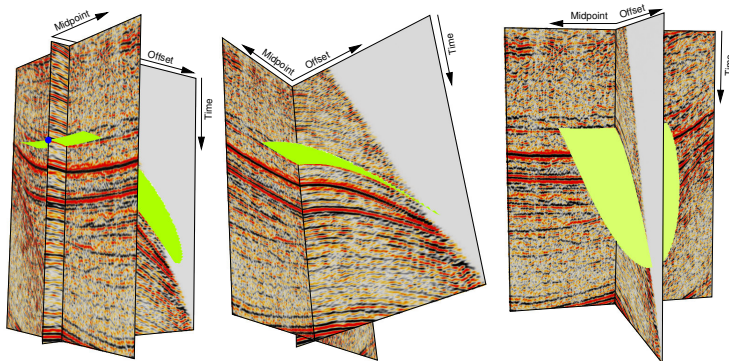
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CRS operator



CMP gather and section at offset 500 m

Displayed ranges: offset up to 3.5 km, midpoint ± 5 km

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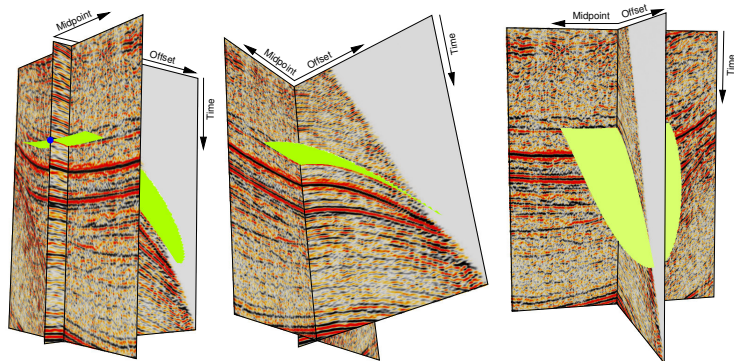
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CRS operator



CMP gather and section at offset 500 m

Displayed ranges: offset up to 3.5 km, midpoint ± 5 km

$$t_0 = 1.5 \text{ s}, \rho = 1.5 \times 10^{-5} \text{ s/m},$$
$$v_{\text{NMO}} = 2015 \text{ m/s}, v_{\text{CMO}} = i \times 9812 \text{ m/s}$$

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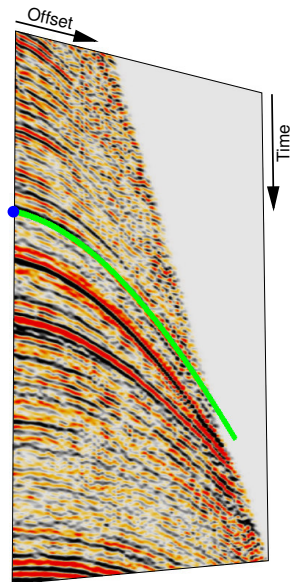
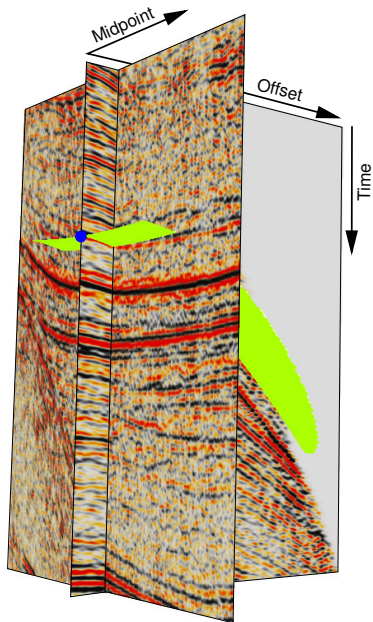
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CRS vs. CMP operator



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What about 3D?

- ▶ prestack data represents a 5D hyper volume

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What about 3D?

- ▶ prestack data represents a 5D hyper volume
 - ▶ offset is now a 2D vector

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What about 3D?

- ▶ prestack data represents a 5D hyper volume
 - ▶ offset is now a 2D vector
 - ▶ midpoint displacement is now a 2D vector

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What about 3D?

- ▶ prestack data represents a 5D hyper volume
 - ▶ offset is now a 2D vector
 - ▶ midpoint displacement is now a 2D vector
 - ▶ CRS stacking operator is a 4D hyper surface

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What about 3D?

- ▶ prestack data represents a 5D hyper volume
 - ▶ offset is now a 2D vector
 - ▶ midpoint displacement is now a 2D vector
 - ▶ CRS stacking operator is a 4D hyper surface
- ▶ Stacking parameters:

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- ▶ general idea remains just the same

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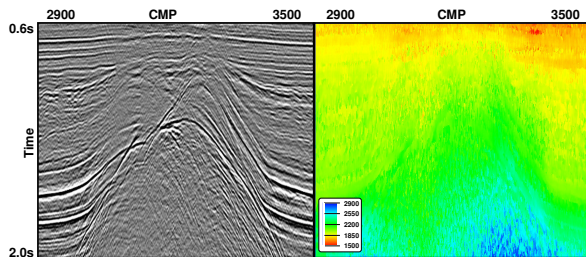
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High density velocity analysis



intermediate stack

stacking velocity

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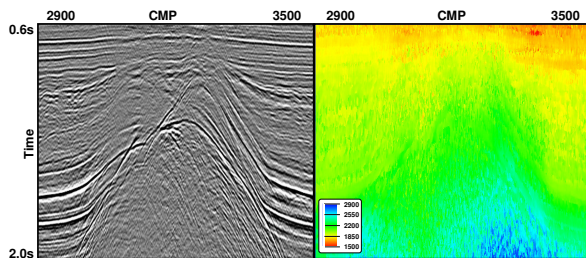
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High density velocity analysis



intermediate stack

stacking velocity

+ fully automated

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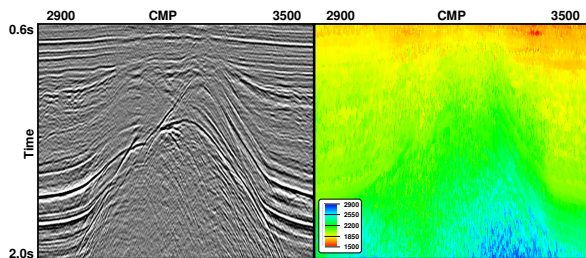
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High density velocity analysis



intermediate stack

stacking velocity

- + fully automated
- + no pulse stretch phenomenon

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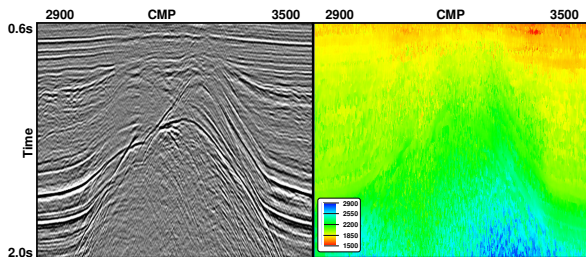
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High density velocity analysis



intermediate stack

stacking velocity

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- + no explicit DMO correction required

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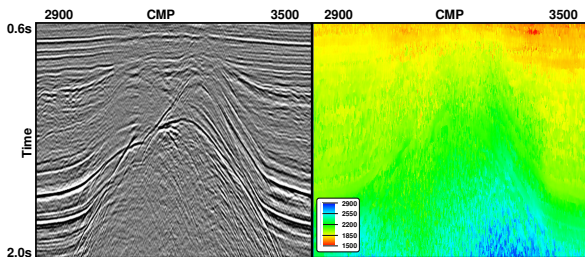
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High density velocity analysis



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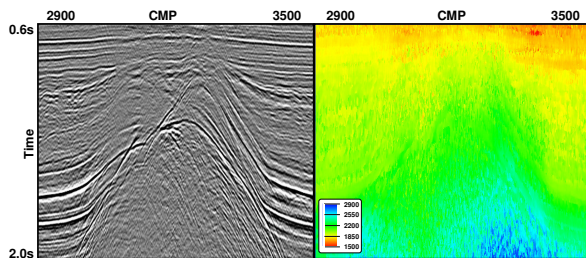
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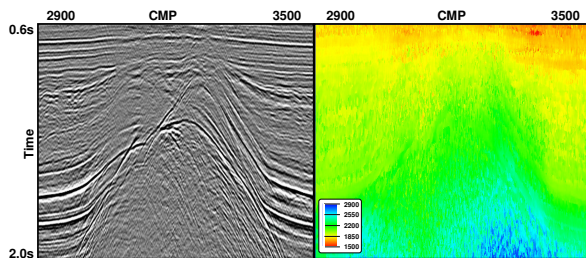
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High density velocity analysis



intermediate stack

stacking velocity

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- no interactive interpretation
- contains outliers and fluctuations
 - ➔ event-consistent smoothing

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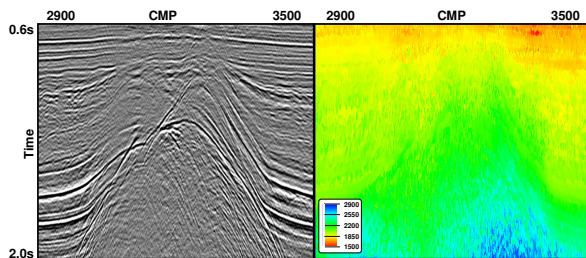
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- contains outliers and fluctuations
 - ➔ event-consistent smoothing
- might pick multiple events

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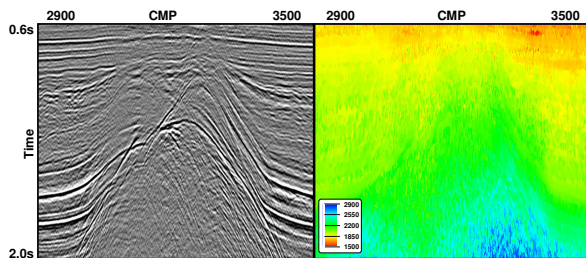
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High density velocity analysis



intermediate stack

stacking velocity

- + fully automated
- + no pulse stretch phenomenon
- + no explicit DMO correction required
- no interactive interpretation
- contains outliers and fluctuations
 - ➔ event-consistent smoothing
- might pick multiple events
 - ➔ smooth reference model plus variation

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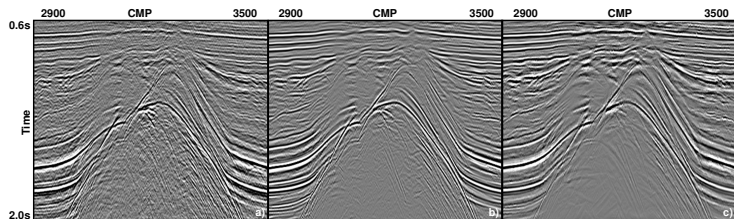
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Midpoint aperture



Detail of a stacked section with

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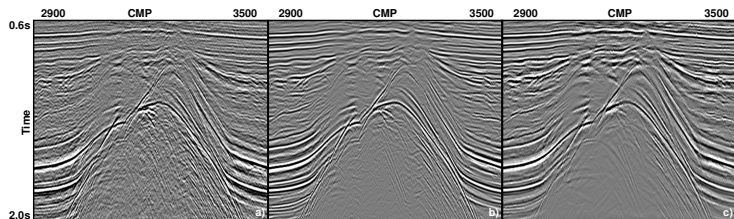
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Midpoint aperture



Detail of a stacked section with

a) zero midpoint aperture (conventional stack)

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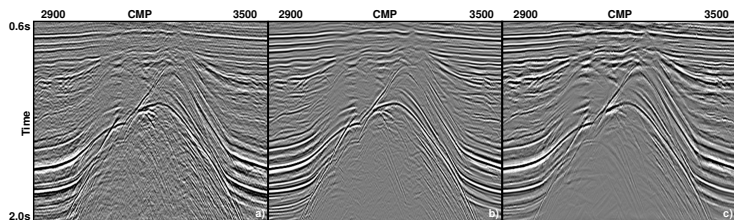
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Midpoint aperture



Detail of a stacked section with

- a) zero midpoint aperture (conventional stack)
- b) estimated size of the projected Fresnel zone

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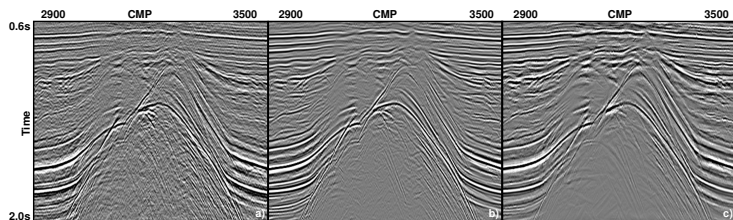
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Midpoint aperture



Detail of a stacked section with

- a) zero midpoint aperture (conventional stack)
- b) estimated size of the projected Fresnel zone
- c) five times larger than in b)

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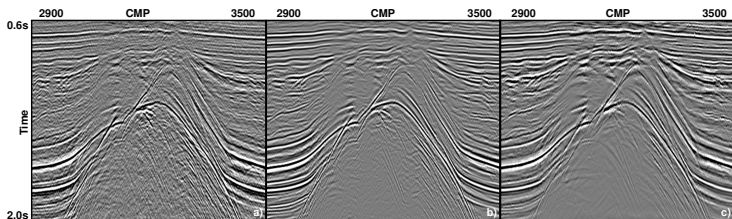
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Midpoint aperture



Detail of a stacked section with

- a) zero midpoint aperture (conventional stack)
- b) estimated size of the projected Fresnel zone
- c) five times larger than in b)

➔ b) is a balance between high S/N ratio, reflector continuity, and resolution

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CRS stack

- ▶ complements conventional methods

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CRS stack

- ▶ complements conventional methods
- ▶ generalization of conventional stacking velocity analysis

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Conclusions

CRS stack

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- ▶ better use of data redundancy

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CRS stack

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 - ▶ velocity model inversion



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 - ▶ geometrical spreading factor

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